Chapter 3:

Simulation of production and elastic properties of reservoirs to validate time-lapse seismics.

3.1 Introduction

Time-lapse, or 4-D, seismic monitoring is an integrated reservoir exploitation technique based on the analysis of successive 3-D seismic surveys. Differences over time in seismic attributes are due to changes in pore fluids and pore pressure during the drainage of a reservoir under production. The detection of areas with significant changes or with unaltered hydrocarbon-indicative attributes can help determine drilling targets where hydrocarbons remain after several years of production.

Making sure that seismic differences are related to fluid flows is critical for a complete time-lapse seismic study. Differences in data acquisition, survey orientation, processing and quality of datasets can introduce significant noise in the 4-D analysis. This can be especially true when legacy datasets are used, which were not acquired specifically for 4D interpretation. Also, to quantify the amount of hydrocarbons responsible for the seismic differences, it is necessary to have a complete petrophysical model of the reservoir to establish a direct relationship between seismic attributes and pore fluids. Such a model can be built by stochastic simulations of the lithology and porosity, which are dependent on the availability and spatial distribution of the well data that are used as reference. Both, the 4D seismic analysis and the petrophysical characterization, require an independent validation or calibration.

In this paper, we describe how reservoir simulation can be used to generate independent impedance maps to validate or constrain time-lapse interpretation of legacy data sets. A complete 4D analysis is an iterative loop where the original interpretation can be refined along the way. First, we summarize the steps preceding the reservoir simulation, including the 3D seismic processing and inversion, and the preliminary timelapse interpretation. We then describe the elastic models, the properties of reservoir fluids and the reservoir characterization that are used to link the impedance volumes to fluid and lithology distribution in the reservoir. A comparison with impedance maps derived by these equations from simple vertical fluid substitution shows how the observed 4D differences indicate complex migrations that require a realistic reservoir simulation. After description of the reservoir simulator, the results of the simulation are finally used to generate impedance maps that can be compared with seismic inversions. To illustrate the different steps of the entire procedure we use the case study of the K8 reservoir, South Timbalier 295, because of its relative simplicity. In the last section, we present a complete 4D analysis of the Eugene Island 330 field whose complex history is representative of enduring Gulf Coast reservoirs (See location of these two fields offshore Louisiana in Figure 3.1)

3.2 The 4D seismic loop

The first steps of the 4D "loop" are described in great details by *He* [1996] and are only summarized here to define the starting point of the reservoir simulation and lithological model used in the simulation.

3.2.1 Registration and normalization of seismic datasets

Until recently, no seismic survey was shot with the specific purpose of time-lapse analysis. Successive data sets over one location were usually collected with different spacing and orientation. In order to differentiate the seismic attributes (amplitude or impedance) between two surveys, it is first necessary to re-locate them on the same grid. This re-location process uses a 3-D interpolation algorithm, that interpolates between the two grids in travel-time, slice by slice. In addition, in order to be able to compare the results of the inversion of two datasets, we perform a normalization of the amplitudes of the surveys, globally with respect to each other first, and by rescaling them both to a proper amplitude by using synthetic seismograms generated from velocity and density logs acquired in the same area [*He*, 1996]

3.2.2 Non linear inversion of successive 3D datasets

Standard 3D seismic interpretation uses generally seismic amplitudes to identify reservoirs. Time-lapse analysis performed on seismic amplitudes has also been shown to allow the identification of migration pathways [*He*, 1996]. However, amplitudes are only proportional to seismic reflectivity, which depends on the relative variability in the elastic properties of the formation, not on the value of these properties. The comparison of 3D amplitude volumes requires wavefield envelope comparison techniques to identify the high-gradient envelop surrounding High Amplitude Regions [*He*, 1996, *Anderson et al.*, 1994] that have to be identified for time-lapse interpretation.

In contrast, seismic impedance (Z) is directly related to the elastic properties of the sediments :

$$Z = \rho V_{p} \tag{1}$$

where ρ is the bulk density and V_p the sonic compressional velocity. ρ is the volumetric average of the density of the different phases (fluids and solids) and V_p can be explicitly expressed as a function of their density and compressibility (see later sections). Also, unlike amplitudes, a simple algebraic subtraction between the impedance volumes at two dates can be directly converted into fluid or pressure changes. A 4-D analysis based on impedance volumes allows a direct qualitative interpretation of seismic changes in terms of fluid substitution or migrations [*He*, 1996].

He [1996] uses a constrained non-lineal inversion technique to estimate the acoustic impedance volumes from each 3D survey. After the seismic datasets have been horizontally stacked, migrated and re-located, each seismic trace is considered as a one-

dimentionnal zero-offest trace. The one-dimensionnal non-linear inversion uses a forward convolution model to compute seismic traces from impedance functions. The implementation of the inversion is based on a modified Levenberg-Marquardt minimization algorithm [*More*, 1977]. The procedure his made fast and robust by using log-derived impedance trends as a priori impedance functions, and by using covariance functions to constrain the objective functions that are minimized during the inversion [*He*, 1996].

3.2.3 Preliminary 4D interpretation of the K8 sand

To illustrate the methodology, we present the results of the successive steps of the 4D analysis of the K8 reservoir in the South Timbalier 295 field, offshore Louisiana (See figure 3.1 for location). It is the uppermost of the three most productive reservoirs in the ST295 field and produced about 350,000 m³ of oil and 150 millions m³ of gas between two 3D surveys shot in 1988 and 1994. The K8 sand (Figure 3.2) is a combination of channelled mid-fan sheet sands lapping on a paleo-high in the east and gently dipping to the South West [*Hoover*, 1997]. It represents a particularly suitable case study in 4D analysis for several reasons: (1) the first 3D seismic survey was shot before production started, providing a reference seismic volume where fluids in place are in hydrostatic equilibrium. (2) The second survey was shot after 5 years of intense production, which should generate profound changes in pore fluid distribution and pressure over the reservoir. (3) Only two wells have been producing between the two seismic surveys (Figure 3.3), which should allow for a relatively simple migration pattern identification in the 4D seismic.

Figures 3.4a and 3.4b show the results of the inversion of the two surveys shot in 1988 and 1994 over K8. The various layers displayed, numbered from top to bottom, follow the structure of the reservoir shown in Figure 3.2b. Each layer has 101×101 data points, distant by 12.5 m and 20 m in the EW direction and NW direction, respectively,

which corresponds to the resolution of the seismic grid after re-location of the two surveys. The difference between the two inversions (Figure 3.4c) shows a global decrease in impedance (red) in most of the shallower layers and updip (NE) from the two producing wells in the deeper layers. Impedance has mostly increased (blue) in the deeper layer of the reservoir between the two surveys. Because the reservoir was originally filled with oil, and the replacement of oil by gas or water respectively decreases or increases the density and the sonic velocity of the formation, Eq. (1) allows a preliminary qualitative interpretation: oil might have been replaced mostly by gas in the shallower layers of the reservoir and by water in the deeper layers. The substitution of oil by gas exsolution updip is controlled by the pressure decrease induced by the producing wells (see pressure drop in Figure 3.3b), while the replacement of oil by water in the deeper layers is assisted by the presence of an aquifer supporting the reservoir [*Tucker*, 1997, *Mason*, 1992].

Independently of the nature of the pore fluid, the bulk of the impedance of such medium porosity sediments (40% maximum) is controlled by the porosity and lithology distributions. To relate quantitatively the observed changes in impedance with the nature and the volume of the pore fluids, it is necessary to have a complete representation of the sediment matrix, and to define the relationships between the different component of the system and its elastic properties.

3.3 Elastic properties of reservoir sediments

3.3.1 Elastic models

Explicit relationships relating pressure, pore fluid, porosity, matrix materials and the elastic properties of marine sediments have been the topic of many studies, some theoretical [*Gassmann*, 1951, *Biot*, 1956, or *Kuster and Toksöz*, 1974], some empirical (*Han et al.*, 1986, *Ramamoorthy et al.*, 1995, *Tosaya and Nur*, 1982]. They are all limited

in application by the infinite number of parameters affecting the elastic properties of sediments and no approach can offer a comprehensive formulation. We reviewed some commonly accepted models and relationships that could be used to link the changes observed in our impedance maps with fluid substitutions in the reservoirs. Most of them define relationships for the elastic moduli of the formation instead of the impedance. The bulk modulus (K) is the inverse of compressibility and the shear modulus (G) is a measure of the shear strength. Compressional and shear (V_s) sonic velocity can be expressed as functions of these moduli and of the density of the sediments:

$$V_p = \sqrt{\frac{1}{\rho} \left(K + \frac{4}{3} G \right)}$$
 (2a) and $V_s = \sqrt{\frac{G}{\rho}}$ (2b)

and the impedance can be re-written

$$Z = \rho V_{p} = \sqrt{\rho \left(K + \frac{4}{3}G\right)} = \sqrt{\rho K + \frac{4}{3}\rho^{2} V_{s}^{2}}$$
(3)

3.3.1.1 Theoretical formulations

Gassmann [1951] and *Biot* [1956] expressed the bulk modulus of fluid-saturated sediments as a function of the bulk moduli of the dry frame (K_f), of the pore fluid (K_{fl}) and of the grains (K_g)

$$K = K_g \frac{K_f + Q}{K_g + Q} \quad \text{with} \quad Q = \frac{K_w (K_g - K_f)}{\Phi (K_g - K_w)}.$$
(4)

This formulation requires the knowledge of the dry bulk modulus, for which *Hamilton* [1971, 1982] established empirical relationships as a function of porosity for several types of lithology. Using his results for clay, silts and fine sands, we define a single formula for clastic sediments:

$$\log (K_f) = \log(K_g) - 4.25\Phi \text{ or } \log(K_f/K_g) = -4.25\Phi.$$
 (5)

The grain modulus of a shale/sand mixture can be calculated by a Voigt-Reuss-Hill average of the grain moduli of sand (K_s) and clay (K_c) [*Hamilton*, 1971]:

$$K_{g} = \frac{1}{2} \left[\gamma K_{c} + (1 - \gamma) K_{s} + \frac{K_{s} K_{c}}{K_{s} \gamma + K_{c} (1 - \gamma)} \right]$$
(6)

where γ is the shaliness or volumetric shale fraction. We refer to it as the Gassmann/Hamilton model [*Guerin and Goldberg*, 1996, Chapter 2]. Values of the grain moduli are given in Table 1.

Kuster and Toksöz [1974] used the theory of sonic waves scattering and propagation to calculate the effective elastic moduli of a two phase medium made of spherical inclusions in a uniform matrix:

$$K = K_{m} \frac{1 + \left[4G_{m}(K_{i} - K_{m})/((3K_{i} + 4G_{m})K_{m})\right]I_{c}}{1 - \left[3(K_{i} - K_{m})/(3K_{i} + 4G_{m})\right]I_{c}}$$
(7)

and
$$G = G_m \frac{(6K_m + 12G_m)G_i + (9K_m + 8G_m)[(1 - I_c)G_m + I_cG_i]}{(9K_m + 8G_m)G_m + (6K_m + 12G_m)[(1 - I_c)G_i + I_cG_m]}$$
 (8)

where the i and m subscripts refer to the inclusion and the matrix properties, respectively, and I_c is the volumetric fraction of the inclusion. This formulation can be extended to a three phases medium [*Zimmermann and King*, 1986, Chapter 2]. In the case of shaly sediments, the grain aggregate is considered a shale matrix with spherical sand grain inclusions ($I_c = 1 - \gamma$). The aggregate is then treated as an inclusion within a fluid matrix ($I_c = 1 - \Phi$). This fluid matrix is considered as a single phase, independently of the possible presence of various fluid types in the pore space.

Unlike the Gassmann/Hamilton model, Eqs. (7) and (8) do not require an empirical expression of the dry modulus, and for this reason could seem of a more practical use. This model (KT) also offers a relationship for the shear modulus, which is required to calculate V_p and the impedance but is not provided by Gassmann/Hamilton. However, it depends on strong assumptions on the shape and arrangement of the grain that can be of limited relevance to describe the grains configuration of the rapidly buried Gulf Coast sediments.

3.3.1.2 Experimental relationships

Underlining the practical limits of these theoretical relationships, particularly regarding the specific influence of clays on sonic wave velocities, *Han et al.* [1986] used shaly sandstone core samples presenting a wide range of porosity and shaliness to define in laboratory the following linear relationships between ultrasonic velocities, porosity and clay content:

$$V_{\rm p} = 5.59 - 6.93\Phi - 2.18\gamma \tag{9}$$

$$V_s = 3.52 - 4.91\Phi - 1.89\gamma \tag{10}$$

They conclude that clay content is, after porosity, the most important parameter affecting the sonic velocity of shaly sediments. In this formulation, both velocities are independent of the pore fluid, and the only effect of pore fluid substitution on impedance is in the density.

Ramamoorthy et al. [1995] note that (9) and (10) and other similar empirical linear relationships fail to describe properly the elastic properties of shaly sediments in some standard lithological conditions. They propose to consider independently the effects of porosity and clay. Using *in situ* data from shear sonic and geochemical logs they give the following relationship for the shear modulus of shaly sediments:

$$G = G_{\text{grain}}(1 - 3.48\Phi + 2.19\Phi^2)$$
(11)

with
$$G_{\text{grain}} = (0.039 \log_{10}(\gamma) + 0.072)^{-1}$$
 (12)

 G_{grain} is the effective grain shear modulus. Eq (11) was originally derived by *Murphy* [1993] from measurements on clean sandstones where G_{grain} was the bulk modulus of pure quartz.

Knowing the limits of any of the above relationships we have to determine which one could be used the most reliably and the most readily for the qualitative interpretation of the time-lapse impedances maps in an integrated 4D analysis. In addition to the properties of the matrix, this requires to formulate also the elastic properties of the pore fluid, which are the primary parameters responsible for changes in impedance during production.

3.3.2 Fluid properties

3.3.2.1 Properties of fluid mixtures

The elastic properties of the pore fluid are in fact the properties of a fluid mixture, which is a function of the properties of the various fluid phases. The three primary types of pore fluid in a reservoir are hydrocarbon gas (gas) hydrocarbon liquid (oil), and brine. The density and the compressibility of the mixture are the weighted averages of the three phases:

$$S_{oil} + S_{gas} + S_{brine} = 1$$
(13)

$$\rho_{\text{fluid}} = S_{\text{oil}}\rho_{\text{oil}} + S_{\text{gas}}\rho_{\text{gas}} + S_{\text{brine}}\rho_{\text{brine}}$$
(14)

$$\frac{1}{K_{fluid}} = \frac{S_{brine}}{K_{bne}} + \frac{S_{gas}}{K_{gas}} + \frac{S_{oil}}{K_{oil}}$$
(15)

where S_{brine} , S_{gas} and S_{oil} are the saturations, or fraction of the pore space, occupied by each phase. Subscripts refer to the attributes of each phase. Equation (13) expresses the presence of only three fluid phases maximum.

3.3.2.2 Elastic properties of reservoir fluids

Batzle and Wang [1992] give a detailed description of the properties of reservoir pore fluids and we only summarize the parameters and principal relationships that can be used in time-lapse analysis. Physical properties of reservoir fluids are dependant on composition, pressure and temperature. Unless thermal recovery techniques are used, the variations of temperature in a reservoir are negligible during its production history, and pressure and composition are the dominant parameters affecting the changes observed between two surveys.

Brine: Brine physical properties are extremely dependant on its salinity (S). In the Gulf of Mexico, the presence of the buried Jurassic salt generates a significant increase of

salinity with depth. In most reservoirs, brine samples are collected and their salinity measured, but *Batzle and Wang* [1992] offer a relationship to estimate salinity as a function of depth that can be used for gulf coast sediments. They also provide relationships for the velocity and density of brine as a function of salinity, pressure and temperature (See Appendix). Brine density and velocity increase with pressure in standard hydrocarbon reservoir conditions.

Gas: The gaseous phase present in the pore space of a reservoir is a mixture of the lightest hydrocarbon fractions. Its composition can vary during production when reservoir pressure decreases and the lightest oil components come out of solution. The properties of the gas mixture can be characterized by the gas specific gravity (G) measured at standard temperature and pressure conditions (15.6°C and 1 atm). If a complete PVT (Pressure-Volume-Temperature) analysis of the physical properties of gas samples is not systematically performed, the measure of its gravity is most often available and allows a good estimation of its properties as function of pressure and temperature [*Batzle and Wang*, 1992]. The formulas in the Appendix show that the density and the bulk modulus of gas mixtures increase significantly with pressure.

Oil: The elastic properties of the 'Oil' phase, or liquid hydrocarbon, are the most complex of the reservoir fluids, but can also be calculated from a few experimental parameters [*Batzle and Wang*, 1992]. In addition to the crude oil produced at the surface, the oil phase in a reservoir can include dissolved light hydrocarbons that are gaseous at lower pressure. One of the key parameters controlling the properties of oil is the bubble point pressure, which is the maximum pressure where free gas can be present. As long as reservoir pressure is above bubble point, oil is under-saturated with regard to gas, its composition remains fixed and the density and bulk modulus both increase with increasing pressure. If reservoir pressure falls below bubble point during production, the lightest dissolved gas start coming out of solution. As pressure decreases and more light component leave the liquid phase, only the heaviest hydrocarbon remain in this phase,

and the density and bulk modulus of the oil phase increase with decreasing pressure [*Batzle and Wang*, 1992, *England et al.*, 1987].

The value of the bubble point and the relationships between pressure and elastic properties should be determined from PVT analysis of actual oil samples. If such analysis is not performed, the values of oil and gas density at surface conditions can be used to determine these relationships and the bubble point pressure [*Batzle and Wang*, 1992, *Beggs*, 1992, see equations in Appendix].

One of the standard indicators of fluid properties is the produced Gas-Oil ratio (GOR), which is the ratio of the volumes of gas and oil produced at the surface. The GOR remains constant as long as the reservoir pressure is above bubble point, but increases as soon as pressure falls below this value and free gas saturation exceeds a critical value, at which point it becomes mobile and gets preferably produced [*Batzle and Wang*, 1992, *Steffensen*, 1992]. This is shown clearly in K8 (Figure 3.3b) by the rapid increase in gas production in well A22 at the beginning of 1993 when reservoir pressure fell below the bubble point at 51.7 MPa. The evolution of the GOR is one of the key control parameters in monitoring production simulation.

3.3.2.3 Original fluids in place

The last aspect of fluid properties affecting the impedance volume is the distribution of the different phases within the reservoir. While one of the goals of the reservoir simulation is to determine the evolution of these distributions during production, the original fluids in place before production can be totally determined from the fluid PVT properties if we assume the reservoir in hydrostatic equilibrium. The density-pressure relationships provide the pressure gradient within each phase and the entire pressure and fluid distributions can be integrated from the knowledge of the depth of the oil-water contact (OWC) and of one pressure value at one depth within the oil or gas zone. Additional parameters necessary for the most accurate distribution include capillary pressures between each phase and the connate water fraction, or irreducible water saturation, which depends on matrix properties and is measured on reservoir samples.

In the case of K8, the original oil-water contact in 1988 was detected at 3350 mbsf, downdip from the study area. The Bottom Hole Pressure (BHP) measured in A-12 at the beginning of production was 57.7 MPa. These two data points and the oil gravity (define the pressure distribution at equilibrium shown in Figure 3.5. Because the lowest pressure was higher than the bubble point (51.7 MPa) no gas was present. Because the OWC was deeper than the lowest point in the study area, water saturation was uniformly equal to the connate water fraction [30%, *Hoover*, 1997] and oil occupied the rest of the pore space (70%).

3.3.3 Stochastic reservoir characterization

The missing link between impedance volumes, fluids properties, saturations and pressure distribution using equations (1)-(15) resides in the characterization of the reservoir porosity and lithology distribution. We use geostatistical simulations for this characterization, assuming that within an individual reservoir petrophysical and acoustic properties are closely related and can be associated with calibrated cross-correlation functions [*He*, 1996]. Using well logs as "Hard" accurate data and impedance volumes as "Soft" data, this method combines the high vertical resolution and accuracy of logs with the wide aerial coverage of 3D seismics. *He* [1996] provides a complete description of the Markov-Bayse conditional soft indicator technique used .

The lithology is expressed in terms of shaliness. The hard data are shale fraction values calculated from Gamma Ray (GR) and Spontaneous Potential (SP) logs in wells distributed across the reservoir. The soft "inaccurate" data, which have to be of the same type, are approximate shaliness values (γ_s) calculated from the impedance volume by a simple weighted average:

$$\gamma_{s} = \frac{Z - Z_{sand}}{Z_{shale} - Z_{sand}}$$
(16)

where Z is the inverted impedance, and Z_{sand} and Z_{shale} are impedance values for pure sand and shale formations. For the porosity distribution, the hard data come from porosity logs, and the soft data are calculated from the impedance volume by a modified timeaverage relationship:

$$\Phi = \left(\frac{Z - Z_{\text{sand}}}{Z_{\text{fluid}} - Z_{\text{sand}}}\right) - \gamma_{s} \left(\frac{Z_{\text{sand}} - Z_{\text{shale}}}{Z_{\text{fluid}} - Z_{\text{shale}}}\right)$$
(17)

where Z_{fluid} is an average brine impedance value [*He*, 1996].

Sixteen wells provided the hard data used to constrain the reservoir characterization of K8 (figure 3.6). Both porosity and shale distributions show a high level of heterogeneity, illustrating the channelled deposition of the reservoir. The bulk of the porosity is located immediately downdip from the two producing wells and in the South East corner of the study area.

3.3.4 From saturation to impedance

The reservoir characterization allows to use any of the petrophysical models (Eqs 4-10) to calculate the impedance volumes when pressure and fluid distributions are known. Having previously established the fluid and pressure distribution before production in K8, we can compare the estimations of the different models with the 1988 impedance inversion to determine which formulation offers a better representation of the observed reservoir properties. Since the Gassmann/Hamilton model (Eqs 4-6) does not provide a value for the shear modulus, we combined this bulk modulus estimate with the shear velocity or moduli expressions of *Han et al.* [1986](Eq. 10), *Kuster and Toksöz* [1974] (Eq. 8), and *Ramamoorthy et al.* [1995] (Eq. 11) to estimate three different impedances values. We refer to these values as the Gassmann+Han, Gassmann+KT and Gassmann+Ramamoorthy impedances, respectively. Two additional impedance volumes were calculated with the complete KT model (Eqs. 7-8) and with the expression of V_p and V_s given by *Han et al.*, [1986] (Eqs 9-10). We refer to these values as the KT and Han impedances, respectively. All the parameters used for grain and fluid properties are given in Tables 1 and 2.

In Figure 3.7, the crossplots of the different models with the 1988 impedance allow to compare their respective validity. In all these figure, a perfect formulation should result in an identical linear fit with the inverted values. The KT and Gassman+KT impedances (Figs 3.7a and 3.7b) display the highest level of scattering and consequently the poorest agreement with the inversion results. The Han and Gassmann+Han impedances present the best agreement with the inversion, with regression coefficients higher than 0.80. This comparison seems to indicate the better readiness of these two formulations to represent the acoustic properties of the reservoir in hydrostatic equilibrium. The impedance distribution calculated with Gassmann+Han is shown in figure 3.8a and compares very well with the 1988 inversion (Fig 3.4a). It will be necessary, however, to make a similar comparison after simulation to evaluate how fluid substitution affects the comparison between the calculated and the inverted impedance.

3.3.5 Comparison with vertical sweep

This preliminary validation of the elastic formulations can be used to illustrate the need for an accurate understanding of the reservoir dynamics that time-lapse seismic can provide. A traditional view of the fluid movements within a producing reservoir is of a uniform buoyancy-driven movement of the different phases, the contact surfaces between adjacent phases remaining horizontal. In the case of K8, where the driving mechanisms are gas ex-solution and a weak aquifer support [*Mason*, 1992], this would mean that the gas/oil contact (GOC) migrates uniformly downdip, as the gas cap expands and more gas come out of solution, while the WOC progresses upwards. Because the BHPs measured in the two wells after 1992 were below the bubble point, this indicates that the GOC has migrated down to at least these depths (3250 mbsf). Assuming that the GOC and WOC

have been simply sweeping uniformly along dip, and that the reservoir is still globally in hydrostatic equilibrium at any time, we have calculated as previously the pressure and fluid distribution that would exist in 1994 if an horizontal gas cap had formed down to 3280 mbsf and the WOC had moved up to 3320 mbsf. The impedances calculated from these values using the Gassmann+Han formulation are shown in Figure 3.8b. Comparison with Figure 3.4b shows that the impedances calculated present strong similarities with the 1994 inversion results. The impedance changes over time (Figures 3.4c and 3.8c) also display some global similarities: decrease in impedance updip from the wells, and increase downdip. However, the pattern and the absolute values of the observed impedance changes are much more heterogeneous in Fig 3.4c than in this simple 'gravitational sweep'. The bright areas in the observed impedance changes correspond to isolated impedance decreases, that could indicate areas with low connectivity where hydrocarbon, mostly gas, would remain trapped as the reservoir pressure decreases. The comparison of Figs 3.4c and 3.8c shows that after a few years of intense production, the representation of a GOC as a continuous horizontal surface is merely irrelevant. The fact that the impedances calculated after the reservoir sweep (Fig 3.8b) compare reasonably well with the inversion results in 1994, despite the major differences in the changes over time (Fig 3.4c vs. Fig 3.8c), shows how crucial it is for each inversion to be the most accurate, as differentiating between the inversions of successive surveys is much more sensitive to errors than either inversion.

3.4 Reservoir Simulation

The entrapment of hydrocarbons is mostly the result of the heterogeneity in the reservoir and in the permeability distribution. Assuming that our inversion results are correct, the heterogeneity observed in the impedance difference over time suggests a migration process more complex than the simple gravitationnal sweep. Numerical simulation of the migration of the different phases can be used to identify the actual behavior of the reservoir under production.

3.4.1 Permeability distribution

In addition to porosity, the primary control on the reservoir drainage is the permeability distribution. While permeability is directly related to porosity, it can also be affected considerably by the presence of shales [*Audet*, 1992, *McCarthy*, 1991]. In clean sands, permeability has been found to be an exponential function of porosity

$$k_{ss} = \alpha \exp(\beta \Phi) \tag{18}$$

where the coefficients α and β can be measured experimentally on core samples. Figure 3.9a shows the exponential regression derived from sidewall core samples collected in K8. The samples used were almost pure sandstone. *McCarthy* [1991] showed that the effects of porosity and shaliness (γ) on the permeability of sand/shale mixtures are independent and that the effective permeability of shaly sandstones is:

$$\mathbf{k} = \mathbf{k}_{ss} \cdot (1 - \gamma)^{m} = \alpha \exp(\beta \Phi). \ (1 - \gamma)^{m}$$
(19)

where m is an exponent dependant on the aspect ratio of the clay minerals. If m = 5, which is a lower bound for the values calculated by *McCarthy* [1991], the presence of only 30% of shale would decrease the permeability by 85%, almost an order of magnitude. The permeability distribution in K8, calculated with m = 5, with the coefficients α and β from Fig 3.9a, and using the porosity and shaliness of Figure 3.6, is shown in Figure 3.10.

3.4.2 Multiple-phase fluid flows in porous media

Reservoir simulation is based on solving the mass conservation equation of multiplephase fluids in porous media, which can be expressed for a finite volume V within a surface A by:

$$\int_{V} \frac{\partial}{\partial t} (\rho_{f} \phi) = - \int_{A} \vec{q} \cdot d\vec{A} + G_{V} \cdot$$
(20)

 G_v is a source term that can encompass the effect of injecting or producing wells. \vec{q} represents the fluid flow per surface unit, according to Darcy's law for multi-phase fluid flows in porous media:

$$\vec{q} = -k. \sum_{\varphi=0,g,w} S_{\varphi} \rho_{\varphi} \frac{k_{r\varphi}}{\mu_{\varphi}} \left[\vec{\nabla} P_{\varphi} - \rho_{\varphi} \vec{g} \right]$$
(21)

where the subscript φ refers to the attributes of each phase (oil, gas, water): saturation (S_{φ}) , pressure (P_{φ}) , density (ρ_{φ}) , viscosity (μ_{φ}) and relative permeability $(k_{r\varphi})$. k is the absolute permeability of the formation and \vec{g} the gravity acceleration.

The relative permeability of each phase increases with its saturation and can be calculated in three phases fluid as a combination of the relative permeabilities of twophases fluid mixtures:

$$k_{ro} = \frac{S_{g}k_{rog} + (S_{w} - S_{wco})k_{row}}{S_{g} + S_{w} - S_{wco}}$$
(22)

where k_{rog} and k_{row} are the oil relative permeability for systems with oil and gas only and oil and water only, respectively. S_{wco} is the connate, or irreducible, water saturation. The variations of k_{rg} and k_{rog} as a function of gas saturation and of k_{rw} and k_{row} as a function of water saturation, called saturation functions, have to be explicitly provided to the simulator. The lower end member of each saturation function is the critical saturation, which is the minimum saturation value for each phase to become mobile. Because of their dependance on the fluid compositions and on the pore structure, saturation functions should be measured in laboratory for every reservoir. However, relative permeability measurements are rarely performed, in part because the experimental procedures to measure them are not universally established [*Rose*, 1992]. No relative permeability measurements were available for either K8 or the Eugene Island LF330 field, and since this absence has to be expected in most reservoirs, saturation functions are among the prime parameters to adjust within the 4D loop. The saturation functions used in K8 are shown in Figure 3.9.

3.4.3 Simulator description

The code used to solve Eq (20) is ECLIPSE, a commercial three phase, three dimensional finite differences simulator using a corner point geometry grid that allows to define highly distorded nodes to represent the reservoir geometry [*Ponting*, 1989]. The position and the shape of each grid block is defined by the coordinates of its eight "corners". The coordinates and the attributes of the grid blocks (porosity and permeability) are directly imported from the reservoir characterization grid. The numerical formulation of Eq. (20) in finite differences for a grid block n connected to a number of blocks m is:

$$\frac{V\Phi}{\Delta t} \sum_{\varphi=o,w,g} \Delta(\rho_{\varphi} S_{\varphi}) = \sum_{\substack{m \\ \varphi=o,w,g}} \left(\frac{\rho_{\varphi} T k_{r\varphi}}{\mu_{\varphi}} \right)_{n,m} \left[P_{\varphi m} - P_{\varphi n} - \eta_{n,m} D_{n,m} \rho_{\varphi} g \right] + (GV)_{n} \quad (23)$$

where the transmissibility $T_{n,m}$ between n and m is calculated by:

$$\frac{1}{T_{n,m}} = \frac{1}{T_n} + \frac{1}{T_m}$$
(24)

$$T_{n} = k_{n} \frac{\vec{A}_{n,m} \cdot \vec{D}_{n,m}}{\vec{D}_{n,m}^{2}} = k_{n} \frac{A_{n,m_{x}} D_{n,m_{x}} + A_{n,m_{y}} D_{n,m_{y}} + A_{n,m_{z}} D_{n,m_{z}}}{D_{n,m_{x}}^{2} + D_{n,m_{y}}^{2} + D_{n,m_{z}}^{2}}$$
(25)

 $\tilde{A}_{n,m}$ is the outbond surface vector for the interface between n and m and $\tilde{D}_{n,m}$ is the vector connecting the center of block n to the centre of the interface.

Since the only actual measurable effects of the reservoir drainage are the volumes of hydrocarbons collected at the surface, the production history recorded on the rig floor is the principal constraint on the simulator. It is expressed in terms of daily production rate of oil or gas for each well, and averaged monthly. This imposed production is translated into pressure gradients between the wellbores and the formation, which are echoed in the reservoir at each time step of the simulation. The flow rate of phase ϕ across an open wellbore interval is

$$Q = TM_{\varphi}(P_{\varphi} - P_{well})$$
⁽²⁶⁾

with T = Connection transmissibility factor = $2\pi kh/ln((r_o/r_w) + S)$

 r_o = pressure equivalent radius of the grid block = 0.14 $(D_x^2 + D_y^2)^{1/2}$

 $M_{\phi} = \text{phase mobility} = k_{r\phi}/\mu_{\phi}B_{\phi}$

where P_{ϕ} is the pressure of phase ϕ in the node containing the connection, P_{well} the pressure in the well at the depth of the connection, k the absolute permeability of the node, r_w the well bore radius, S the skin factor representing the effect of formation damage, partial penetration or well deviation, D_x and D_y are the horizontal dimensions of the grid block and B_{ϕ} is the formation volume factor of phase ϕ , or its volumetric change from surface to reservoir conditions.

In addition to the perforated well intervals, the only flows allowed in and out the reservoir model are from eventual aquifers. The strength of the aquifer support is defined in water influx per unit pressure difference. All other model boundaries are considered impermeable, either lithologically (shaled out) or structurally (sealing faults).

By default, ECLIPSE uses a fully implicit solution procedure to solve Eq. (23), but in the case of regular grids and short time steps, the IMPES method (Implicit Pressure, Explicit Saturation) can be used for faster and less dispersive simulation but is more unstable than the default fully implicit formulation [*Coats*, 1992].

3.4.4 Simulation of K8

3.4.4.1 Constraint on the simulation: production history analysis

The production history imposed on K8 during the simulation was the oil simulation shown in Figure 3.3a. A-12 was the only producing well from September 89 to June 1992. The primary control of the success of the simulation was to reproduce the gas production and pressure evolution histories (Figures 3.3b). The parallelism between oil

and gas production before 1993 shows that during this period reservoir pressure was above bubble point and reservoir oil was undersaturated with a constant GOR. At the beginning of 1993 the increase in gas production relative to oil production indicates that gas started coming out of solution and that the reservoir pressure in the vicinity of the wells was below the bubble point (51.7 MPa). This gas exsolution is most likely responsible for the decrease in impedance observed between the two seismic surveys in most of the upper layers of the reservoir and updip from the wells .

3.4.4.2 Simulation results

3.4.4.2.1 History match

Figure 3.11 shows how the simulator was able to reproduce the production history of K8, starting from the initial conditions determined in 1988. Dots represent observed production data (from Fig 3.3) and the lines the simulation results. Because oil production was the imposed control mechanism, the perfect match for this production was expected. The poorer match in gas production (Fig 3.11b) indicates that we were not able to reproduce the exact evolution of K8, despite the good agreement of the simulated reservoir pressure (black line in Fig 3.11c) with the few pressure measurements available (black dots). The significant difference in the simulated pressures between the average field pressure and the BHPs of the producing wells shows the artificial pressure drawdown in the wells generated by intense production. The spikes in the simulated A12 BHP correspond to short periods where this well was shut down and the borehole started re-equilibrating with the surrounding reservoir conditions.

Even without matching the exact production history, the simulation helps to understand the dynamics in the reservoir. Figure 3.12 shows the simulated oil streamlines at various times in the simulation. In May 1992, A-12 is the only well producing, and all streamlines converge towards this well. In January 1993, shortly after the beginning of production in A22, some of the streamlines are heading for this well, but the main flow is still bypassing A22 downdip, towards A12. At the two later time steps, the streamlines become equally focussed on the two wells. As long as A12 was the only producing well, migrations occurred mostly in the center of the reservoir. The activation of A22 drove the oil in the western part of the reservoir to flow downdip (to the south) before heading west across the bulk of the reservoir towards the wells. This counter-buoyancy drive requires a consequent pressure drawdown in the south, confirmed by the evolution of the pressure field in Figure 3.13.

3.4.4.2.2 Fluid saturations and impedance

Figure 3.14 shows the oil and gas distributions at the end of the simulation, which have to be compared with the uniform values of 70% oil and no gas at the origin of the simulation. Figure 3.15 shows the impedance volumes and changes over time calculated with these values using the Gassmann+Han formulation. The simulated impedance distribution in 1994 (Figure 3.15b) seems very similar to the inversion results at this date (Fig 3.4b), but to confirm that this relationship still offers the best representation of the reservoir properties after fluid substitutions, we also calculated the impedances after the simulation with the other petrophysical formulations. Figure 3.16 shows the crossplots comparing the different model predictions to the 1994 inversion. As before production, the KT and Gassmann+KT results display the poorest agreement with the inverted impedance, showing even a lower correlation in 1994 than at the origin of the simulation. Figs 3.16c and 3.16d confirm that the impedances calculated with Han and Gassmann+Han still present the best comparison with the inverted impedance after fluid substitutions. A crossplot between the two inversion results (Figure 3.16f) shows that the regressions between the 1994 impedance and the Han and Gassmann+Han models at this date are better than the comparison between the two impedance volumes. This indicates that the errors in the elastic formulations are lower than the changes that they are supposed to quantify, which is a prerequisite for any meaningful quantification. As a step of the 4-D analysis loop, similar comparison between various models should be performed for any reservoir, because some formulations might be more appropriate for different depths, pressures or lithologies. For the K8 sand, and for the LF330 reservoir which has a very similar lithology, the combination of Gassmann/Hamilton and Han were the most suitable.

The comparison of the observed impedances changes over time (Figure 3.4c) with the simulated gas saturation and impedances changes (Figures 3.14b and 3.15c) confirms that the impedance decrease observed directly updip from the wells corresponds to an increase in gas saturation. The impedance decrease in the simulation results does not extend as broadly in the NE part of the reservoir as in the inversion differences. The decrease indicated by the inversions in this area can actually be caused by the production and the gas exsolution in the underlying K16 reservoir which merges with K8 at the crest of the structure. In the SW of the reservoir, downdip from the wells, the results of the simulation indicate a stronger decrease in impedance than observed from the inversion. This simulated decrease is generated by 10 to 15% free gas that came out of solution in this low-porosity part of the model (Fig 3.14b). This could show that the connectivity is higher in this area downdip from the bulk of the reservoir than in our reservoir characterization. Instead of remaining trapped in this corner most of the ex-solved gas should migrate updip to the wells. A higher gas relative permeability could also allow a more efficient mobilization of the gas. In any case, the considerable gas exsolution prevents the oil from being effectively drained in the deeper layers (Fig 3.14a), and a possible way to recover this oil would be to increase the pressure to re-dissolve the free gas. A program was initiated in 1997 for this purpose by injecting water downdip from the oil-water contact [Anderson et al., 1998]. To recover hydrocarbon which are bypassed in the migration shown in Fig 3.12, both simulation results and inversions indicate that the eastern flank of the reservoir could still contain large amounts of unproduced hydrocarbons.

3.5 LF sand, Eugene Island 330

The production history match is not perfect and the differences between simulated and inverted impedances changes show that our analysis of K8 needs refinement, but such discrepancies have to be expected when putting together so many types of data and disciplines in an integrated interpretation. Reducing or explaining the discrepancies is the object of the following steps of the 4D interpretation before spudding a new well.

The case of the LF reservoir, Eugene Island Block 330, is more complex, because of a much longer production history (more than 20 years), and more producing wells (14). It will underline the difficulties in time-lapse analysis and the need for an integrated multidisciplinary iterative loop to optimize the 4D interpretation.

3.5.1 Geological setting and history

The LF sand is one of the most productive reservoirs in the Eugene Island 330 (EI330) field, the world's most prolific Pleistocene oil field [*Anderson et al.*, 1993], 200 km South-West of New Orleans (Figure 3.1). Because of its exemplary longevity, EI330 has been one of the most thoroughly studied fields in the Gulf of Mexico since its discovery in 1971. It has been the object of multiple seismic surveys and provided a large amount of core and log data, making it a typical case for petrophysical characterization and time-lapse interpretation. The more than 25 sands that constitute the field are stacked under rollover anticlines within an active growth fault system. Down-to-the-basin and antithetic faults have divided the field into several fault blocks, sealing laterally individual sand compartment to form a total of more than 100 separate reservoirs [*Holland*, 1991]. The LF sand is a Pleistocene distributary-mouth bar deposit, thickening

progressively from the shaled out crest of the anticline on the East to about 40 meters to the West. The top of the reservoir dips gently 10-20° to the west, from 1900 mbsf at the crest to 2300 mbsf (See Figure 3.17).

The 3 x 2 km study area is centered on the boundary between Blocks 330 and 331 within the fault block B of the Red Fault system [*He*, 1996]. In this compartment alone, 14 wells have produced 2.75 million m³ of oil and 550 million m³ of gas since 1972. While production has been slowing down over the years, the depletion rate has been particularly slow (Anderson et al, 1993), and the four wells still producing after 1985 recovered 130,000 m³ of oil and 40 million m³ of gas between the two 3D surveys of 1985 and 1992 (Figure 3.18)

3.5.2 Preliminary 4-D impedance analysis

The results of the seismic impedance inversions in 1985 and 1992 are shown in Figure 3.19. Because of its greater quality, the 1992 survey was used as the base for the re-bining before inversion, resulting in a spacing of 23 m along the dip direction, 15 m along strike and 1.0 m vertically, for a total grid dimension of 134×125×61 nodes. In the two inversions, the lowest impedances are found in the bulk of the reservoir (layer 24 in Fig 3.19), where the higher porosity reinforces the influence of fluid distribution on the elastic properties.

The subtraction of the two impedance volumes in figure 3.19c shows the changes that occurred during the seven years between the surveys. In the upper layers, impedance has decreased almost uniformly, likely because of continuous pressure decrease and gas exsolution. In the deeper layers, impedance generally increased as water was replacing oil, except in two locations: on the northern edge of Block 330, where A-12 was reactivated in 1991 to produce mostly gas and where A-6 and A-8 were active until 1988,

and in a large area centered on the block line downdip from well B4, which was the most productive well during this period. The lateral extent of this "brighter" area decreases with depth, but it extends surprisingly far downdip in Block 331, where no well was active between the two surveys.

3.5.3 Reservoir characterization of LF330

He [1996] used GR and SP logs from 20 wells to calibrate the geostatistical characterization of the lithology, using the 1992 impedance volume as soft data. Because only a few porosity logs were available in Block 330, it was not possible to use an independent geostatistical simulation to determine porosity distribution. Instead, porosity was calculated with the time average relationship (Eq. 17) and the results of the lithology characterization. The resulting lithology and porosity distributions are shown in Figure 3.20. Because of the absence of log-derived correlation functions, the porosity distribution inherits the low spatial correlation of the impedance volume, which prevents from identifying eventual high porosity channels and results in a porosity generally lower than the actual reservoir values (see porosity values of clean samples in Fig 3.21). Permeability measurements on 250 core samples (Fig 3.21) were used to establish the permeability-porosity relationship in the LF sand. The effective permeability distribution (Figure 3.20c) was calculated with an exponent m = 2 for the shale fraction in Eq. (19).

The resolution of the impedance volume was upscaled by 3 in the reservoir simulator, resulting in a grid of $33 \times 33 \times 20 = 21780$ nodes, with dimensions 69 m × 45 m × 3 m. In the upscaling process, both porosity and shaliness were calculated by volumetric average, and the permeability of each node in the model was calculated with the averaged attributes in Eq. (19).

3.5.4 Fluid properties and initial conditions

Because at the time of the first 3D survey (1985), the reservoir had already been producing for 13 years from 14 wells, the distribution of the fluids in place was too complex to assume proper initial conditions for the reservoir simulation at this time. Eventhough the period of interest was within the last seven years, it was necessary to start the simulation from the only fluid distribution that could be determined reliably, which was the hydrostatic equilibrium before production. The OWC and GOC were identified in 1972 at 2320 m and 2050 m respectively [*Holland*, 1991]. The location of the GOC at the crest of the anticline indicates that the upper part of the reservoir was at bubble point pressure (28.5 MPa) before the beginning of production. The other PVT parameters measured on LF hydrocarbon samples and used to calculate reservoir fluid properties are in Table 2. From these data we integrated the initial pressure and fluid distribution in 1972 in the same manner as for K8.

3.5.5 Simulation results

The results of the production and pressure history match in blocks 331 and 330 are shown in Fig 3.22. In block 331 (Figs 3.22a and 3.22b), where most wells produced only until 1977, the simulated productions (lines) match almost perfectly the recorded data (diamonds). The good oil production match was forced as the engine of the simulation. Because of the greater depth in this part of the reservoir and of its short production activity, the pressure remained close to bubble point in most of Block 331 during its producing history. Consequently, gas saturation never exceeded the critical gas saturation value and gas production remained almost proportional to the oil production with constant GOR. The most significant mismatches in block 331 occur with wells A3 and A5, where the simulation does not reproduce the gas production increases observed in 1975. This increase indicates that at this time the gas cap must have reached A3 and A5,

the most updip producing wells of Block 331. The simulation is therefore lagging reality in the extension of the gas cap. However, the good reproduction of the pressure evolution in the field (Fig 3.22e) shows that the mismatch could be related to errors in connectivity in the vicinity of the wells, while the reservoir is behaving properly overall.

In Block 330 (Figs 3.22c and 3.22d), the presence of the gas cap at the onset of production makes the relative productions of oil and gas depend intimately on the correct evolutions of the local pressure fields and of the saturations of the different phases which controls the relative pemeabilities. Volumes of oil produced are usually more accurately recorded than gas production, and are consequently more reliable constraints for the reservoir simulation. However, we were able to get a better cumulative oil and gas match by forcing gas production instead of oil in two wells: A-12 and A-6. Forcing oil production in these wells resulted in gas production much lower than observed, the oil and gas production remaining proportional to each other. This could show that porosity, and permeability, are lower in the vicinity of these wells than estimated from our timeaverage relationship. With lower formation permeabilities, the pressure gradients required to produce the same amount of hydrocarbon would be higher, generating lower pressures around the wells, and therefore higher produced gas/oil ratio. The uncertainty in the porosity estimation is a direct consequence of the lack of reliable well data in the northern part of Block 330 where A-6 and A8 are located [He, 1996]. However, the good reproduction of the pressure evolution (Fig 3.22e) and the overall good match of the most of the wells production suggest that we reproduced reasonably well the volumes of the different phase migrations. In particular, the very good match for Block 331 and the good match in Block 330 in the first years of the simulation indicate that the conditions in the field at the time of the first survey should be similar to the results of our simulation in 1985.

The results of the simulation in terms of oil and gas saturations at the time of the two surveys are shown in Figure 3.23 and 3.24. The comparison of gas saturation and inverted impedance changes shows that the impedance decrease observed in the shallower part of the reservoir between the two surveys can be associated with an increase in gas saturation. Figure 3.24c shows that, despite the absence of production activity in Block 331 between the two surveys, the gas cap kept extending downdip in this block, confirming our preliminary impedance interpretation. However, this qualitative association between gas increase and impedance decrease does not translate quantitatively in the impedance distribution and impedance changes calculated from the simulation results (Fig 3.25). Both impedance volumes calculated in 1985 and 1992 appear generally similar to the inversion results, but the discrepancies between simulation and inversion are apparent when comparing the simulated and inverted impedance changes over time (Fig 3.19c vs. 3.25c). By removing most of the contribution of the matrix materials to the impedance, the differentiation between successive results is much more sensitive to possible disagreements between simulation and inversion. In particular, while the inversion results indicate a decrease in impedance at all depths in the central part of the reservoir (Fig 3.19c), this decrease is limited to the upper layers and the deeper layers in the simulation, where porosity and permeability are low and free gas coming out of solution remains trapped. In the bulk of the reservoir (see layer 8), the simulation results show an increase in impedance associated with oil replacing some of the free gas. Because of the relatively low production between the two surveys, the pressure decrease generated by production is balanced by the return to normal pressure in the reservoir after years of intense production. Figure 3.22e shows that between 1985 and 1992, the average field pressure decreased only slightly, while BHPs across the field increased after having been drown to values much lower than formation pressures. Although the impedance decrease interpreted from the inversion results at the center of the reservoir is clearly identifiable in Fig 3.19c, its amplitude is difficult to explain with only one well producing in the area (B4) at a rather sow rate (about 25 m³/day). Such inconsistencies between seismic inversion, reservoir simulation and actual production data are at the core of the 4-D optimization loop.

3.6 Discussion - End of the 4D loop

3.6.1 Discussion of the LF sand results

Some of imperfections of the LF simulation have to be attributed to the simplified porosity determination. A close look at the two survey times indicates that the agreement between inversion and simulation is better in 1992 than in 1985. This is due to the fact that the porosity distribution was explicitly derived from the 1992 inversion by a simple time average formulation. A qualitative comparison of the 1992 impedance inversion (Fig 3.19b) with the porosity distribution (Fig 3.20a) shows that the porosity pattern can be directly mapped on the 1992 impedance. Such direct relationship between reservoir characteristics and seismic attributes introduces a clear bias in the ability of the simulation to provide an independent validation of the 4D interpretation. For comparison, the porosity distribution in K8 (Fig 3.6a), which was calculated by a complete log-constrained stochastic characterization, cannot be directly mapped on any of the two impedance inversions (Fig 3.4).

Independently from this clear bias in the 1992 impedance match, the poor reproduction of the impedance changes in the LF sand underline the difficulties of timelapse analysis. The only actual constraints on the progress of the simulation are the well production histories and the few pressures recorded, which are very localized data. It is therefore crucial to have reliable inversion results and a complete stochastic reservoir characterization for a precise volumetric reference at the time of the surveys. In the case of the LF sand, because the 1985 survey was acquired a time when 3D seismics were still in their infancy, it does not provide such dependable reference. The original time-lapse analysis of the LF sand was performed through the comparison of region-grown volumes [*He*, 1996]. This technique allowed the identification of migration patterns and a preliminary interpretation of the reservoir dynamics but can not be used for a quantitative estimation of the changes in the reservoir fluids distribution. The subtraction of the two impedance volumes that we use for our qualitative evaluation is much more sensitive than region-growing algorithms to the effects of differences in the acquisition of the two surveys. The low level of confidence in the 1985 impedance added to the inability to constrain the stochastic porosity simulation and to the recurrent absence of parameters such as relative permeabilities make the problem become clearly under-determined in this reservoir.

3.6.2 Closing the 4D analysis loop - optimization

Improving the present results and, more generally, the optimization of the 4D interpretation loop can take several forms. Different sources of uncertainty have been identified, in particular: (1) various numerical parameters and missing reservoir properties, (2) the numerical formulation of reservoir petrophysical properties and (3) results from steps preceding the reservoir simulation, such as seismic inversion and reservoir characterization.

Recurrently missing properties and numerical parameters such as relative permeability functions, critical saturations, capillary pressures, aquifer strength or the shale exponent in the effective permeability calculation can be varied between successive simulations in order to find a better history match. Upscaling the reservoir model dimensions for shorter computation times, it is possible to automate the variation of some of these arbitrary numerical parameters or loosely constrained properties to minimize the difference between measured and simulated production history.

The choice of the most representative petrophysical formulation (Han, Gassmann, KT or others) is crucial to establish the correspondence between impedance inversion and fluids in place. In addition to the formulation themselves, the elastic parameters of the grain matrix in these formulations can be varied to represent different lithologies and grain arrangements. The simple comparison between various formulations such as the crossplots used for K8 (Figures 3.7 and 3.16) can be improved by iteratively varying grain elastic parameters in order to improve the regressions. The relatively limited number of parameters in these formulations can allow simple automated optimization routines to identify the most appropriate model and the proper matrix properties.

Limiting the optimization to the identification of these parameters or to the choice of the petrophysical representation requires that more fundamental components of the 4D interpretation are dependable, in particular the impedance inversions and the reservoir characterization. Reservoir simulation can be used either to validate these prior results, or to constrain their re-evaluation. In the case of LF330, a major source of inaccuracy is the porosity distribution. In the absence of additional logs, a possible way to improve the porosity distribution is to use the simulation results to re-estimate the porosity from the 1992 inversion with the time-average relationship (Eq. 17) and the fluid distribution resulting from the simulation [He et al., 1998]. For all the imprecisions still resulting from the absence of stochastic parametrization and from possible errors in the simulation, the porosity calculated with these simulated saturations should be more appropriate than the uniform average "brine impedance" originally used. This procedure can be used more generally when no survey was shot before production and no reference survey with known hydrostatic fluid distribution provides a reliable reference such as in K8. This would provide a more accurate "soft" porosity distribution for the reservoir characterization.

In addition to the uncertainties in porosity distribution, the analysis of the LF sand is also impaired by the limited confidence in the 1985 seismic dataset. While the steady improvement of 3D acquisition techniques over the last few years has greatly reduced this source of concern for recently acquired datasets, it remains a primordial issue when using legacy datasets which were not acquired along the rigorous guidelines required by time-lapse seismic. The assessment of this uncertainty and of possible remedies requires to go beyond the parameters directly associated with the reservoir simulation. It requires to complete the 4-D analysis by returning to the initial steps of the interpretation loop and to the original data: seismic amplitude volumes.

To complete the loop, the impedance volumes calculated from the results of the reservoir simulation have to be fed into a 3D seismic waves propagation elastic model to try to reproduce the observed datasets. For this purpose, we have built tools allowing to remesh the simulation grid within the original data volume [Mello et al., 1998] and developed a full elastic 3D finite difference model to simulate the propagation of seismic waves and generate a synthetic seismic amplitude volume. The comparison of the simulated amplitudes with the original datasets can be used as a simple validation of the reservoir simulation, but it can also be used to re-evaluate the inversion or the reservoir characterization results when data are missing or unreliable. In the case of the LF sand, the impedance changes calculated from the reservoir simulation are much smaller than indicated by the subtraction of the two inversions. The reservoir simulation and the impedances calculated from its results might be only partially accurate, but since the simulated production volumes and pressure variations were equivalent to the actual production data, the range of the simulated impedance changes should be representative of the actual changes between the two surveys. If we assume that the 1992 inversion is the most accurate, this shows that the 1985 inversion has to be re-estimated. This can be done by applying the 3D elastic model to the 1985 simulated impedances. If the resulting seismic amplitudes volume compares well with the original 3D survey, the simulated impedances can be used as a new *a priori* impedance distribution for the re-evaluation of the inversion of the 1985 survey. Because most of the production occurred before the first 3D survey, the few wells producing after 1985 have merely been developing features of the earlier production phase. Therefore, properly simulating the reservoir before 1985 is as crucial to our time-lapse analysis as the simulation between the two surveys. This can only be completed by a good agreement between seismic inversion, reservoir simulation and elastic simulation at the time of this first survey.

3.7 Conclusion

These are mere possibilities for the 4D interpretation to proceed from reservoir simulation to get an exact understanding of the reservoir dynamics. Because the exploration, production history and the configuration of each reservoir are unique, there is no exhaustive procedure for time-lapse monitoring. We have tried to develop an integrated series of tools allowing to apply our general methodology to any reservoir, but its flexibility requires a clear understanding of the possible sources of errors in order to use the iterative procedure to minimize them.

At the junction between complex theoretical methods (non-linear seismic inversion, 3D elastic modelling or stochastic simulation) and the most primary field data, reservoir simulation provides the link between the observed changes in seismic attributes, the hydrocarbons produced on the rig floor and the actual fluid dynamics within a reservoir. Because it should ultimately indicate where to drill to recover trapped hydrocarbon, and the volumes to expect, it can help understand the passed history of a reservoir, but more importantly, how to make the best of its future. In the case of the K8 sand, the good agreement between simulation and inversion indicate that the final optimization should be only a refinement of the present results. Because of its more complex history and of the lesser quality of the available data, the complete assessment of the future of the LF sand requires a more profound overhaul of our original assumptions.

Completing our conclusions of chapters 1 and 2, we have shown how different types of elastic formulations can be used to quantify transformations of the pore space and of the pore materials in marine sediments. In the case of silica diagenesis and gas hydrate formation, these models allowed to describe the nature of the transformation of the pore space and understand very distinct seismic signatures of long-range processes. Their application to fluid substitutions in a producing reservoir can have direct short term implications: the spudding of a new well. In the last chapter, we describe how temperature and heat flow measurements can be used to identify the long term migrations in active fault zones feeding the LF sand and similar reservoir as we exploit them.

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| Grain type | ρ (g/cc) | V_{p} (m/s) | V_{s} (m/s) | K (.10 ⁹ Pa) | G (.10 ⁹ Pa) |
|------------|---------------|---------------|---------------|-------------------------|-------------------------|
| Clay | 2.6 | 3400 | 1600 | 21.2 | 6.666 |
| Sand | 2.7 | 5980 | 4040 | 38.0 | 44.0 |

 Table 1: Elastic properties of matrix materials.

 Table 2 : Properties of the reservoir fluids used in the simulation and in the elastic models

| Parameter | K8 (ST295) | LF (EI330) | |
|-------------------------------|-----------------------|-----------------------|--|
| Temperature | 88.9°C | 71°C | |
| Bubble point pressure | 51.7 MPa | 28.5 MPa | |
| Gas Gravity (relative to air) | 0.6112 | 0.6953 | |
| Oil density) | 0.855 g/cc (34.0 API) | 0.839 g/cc (37.2 API) | |
| Original OWC | 3350 mbsf | 2320 mbsf | |
| Original GOC | N/A | 2050 mbsf | |
| Connate water saturation | 30% | 40% | |
| Critical gas saturation | 5 % | 20 % | |
| Critical Oil saturation | 20 % | 20% | |

Appendix: Reservoir fluids properties

In an ideal time lapse analysis, a complete PVT analsis of reservoir fluid samples should provide the exact relationships between reservoir fluid properties, pressure and saturation. The main parameters required for the simulation and for calculating impedances are mostly compressibility, density, viscosity. In a typical case only some of these relationships are actually measured, and only a few parameters are systematicaly measured. *Batzle and Wang* [1992] provide a very complete description of the elastic properties of reservoir fluids. We summarize here the few relationships that can be readily used in a typical 4D analys using only the few parameters that are systematically measured: the oil and gas gravities, reservoir temperature and pressure. In all the following relationships, Temperature is in °C, Pressure in MPa, density in g.cc⁻¹ and bulk modulus in MPa.

Brine properties:

In most reservoirs, brine samples are analysed for such purposes as logs calibration or reservoir evaluation. In the absence of brine samples, a linear fit to the data compiled by *Batzle and Wang* [1992] provides a way to estimate salinity (S) vs. depth (z, in m):

$$S = 1.4 \times 10^{-4} z - 0.2 \tag{22}$$

where S is in weight fraction of Sodium Chloride.

The density of water ρ_w can be approximated by a polynomial function of pressure and temperature:

$$\rho_{w} = 1 + 10^{-6} (-80T - 3.3T^{2} + .00175T^{3} + 489P - 2TP + .016T^{2}P - 1.3 \ 10^{-5}T^{3}P - 0.333P^{2} - 0.002TP^{2})$$
(23)

and the brine density is:

$$\rho_{\text{brine}} = \rho_{\text{w}} + S[0.668 + 0.44S + 10^{-6}(300P - 2400PS + T(80 + 3T - 3300S - 13P + 47PS))]$$
(24)

The sonic velocity in pure water has been studied by *Wilson* [1959], who provided the following relationship:

$$V_{w} = \sum_{i=0,4} \sum_{j=0,3} w_{ij} T^{i} P^{j}$$
(25)

where the parameters w_{ij} are given in the following table:

| | i = 0 | 1 | 2 | 3 | 4 |
|-------|-------------------------|-------------------------|-------------------------|-------------------------|--------------------------|
| j = 0 | 1402.85 | 4.871 | -0.04783 | 1.487×10^{-4} | -2.197×10 ⁻⁷ |
| 1 | 1.524 | -0.0111 | 2.747×10 ⁻⁴ | -6.503×10 ⁻⁷ | 7.987×10^{-10} |
| 2 | 3.437×10 ⁻³ | 1.739×10 ⁻⁴ | -2.135×10 ⁻⁶ | -1.455×10 ⁻⁸ | 5.230×10 ⁻¹¹ |
| 3 | -1.197×10 ⁻⁵ | -1.628×10 ⁻⁶ | 1.237×10 ⁻⁸ | 1.327×10^{-10} | -4.614×10 ⁻¹³ |

Gas properties:

Gas mixture properties can characterized by their specific gravity, G, which is the ratio of the gas density to air density at standard conditions.

For temperatures and pressures typically encountered in oil fields, the gas density (ρ_g) and bulk modulus (K_g) can be calculated by:

$$\rho_{\rm g} = \frac{28.8 {\rm GP}}{{\rm ZR}({\rm T} + 273.15)} \tag{26}$$

$$K_{g} = \frac{P}{\left(1 - \frac{P_{pr}}{Z} \frac{\partial Z}{\partial P_{pr}}\right)} \gamma_{o}$$
(27)

where R is the ideal gas constant (R = 8.31 SI) and Z is the compressibility factor, which is a measure of the departure from the ideal gas law that can be measured on samples or approximated by:

$$Z = [0.03 + 0.00527(3.5 - T_{pr})^{3}]P_{pr} + (0.642T_{pr} - 0.007T_{pr}^{4} - 0.52) + E$$
(27)

with
$$E = 0.109 (3.85 - T_{pr})^2 \exp \left\{ - \left[0.45 + 8 \left(0.56 - \frac{1}{T_{pr}} \right) \right] \frac{P_{pr}^{1.2}}{T_{pr}} \right\}$$
 (28)

$$P_{pr} = \frac{P}{(4.892 - 0.4048G)}$$
 and $T_{pr} = \frac{(T + 273.15)}{(94.72 + 170.75G)}$. (29)

and
$$\gamma_{o} = 0.85 + \frac{5.6}{(P_{pr} + 2)} + \frac{27.1}{(P_{pr} + 3.5)^2} - 8.7e^{-0.65(P_{pr} + 1)}$$
 (30)

Oil properties

The properties of oil vary differently wether pressure is higher or lower than the bubble point. In any case, if PVT analysis results are not available, elastic properties can be calculated from its density ρ_0 at standard surface condition, the gas gravity G and the bubble point pressure. Oil gravity is usually expressed by its American Petroleum Institute (API) gravity:

$$API = \frac{141.5}{\rho_0} - 131.5 \tag{31}$$

Above bubble point, the composition of the oil phase remains constant with varying pressure, and the density and velocity can be expressed by:

$$\rho_{\text{oil}} = \frac{\rho_{\text{o}} + (0.00277 \,\text{P} - 1.71 \times 10^{-7} \,\text{P}^3)(\rho_{\text{o}} - 1.15)^2 + 3.49 \times 10^{-4} \,\text{P}}{(0.972 + 3.81 \times 10^{-4} (\text{T} + 17.78)^{1.175})}$$
(32)

$$V_{\text{oil}} = 2096 \sqrt{\frac{\rho_o}{2.6 - \rho_o}} - 3.7T + 4.64P + 0.0115(4.12 \sqrt{\frac{1.08}{\rho_o} - 1} - 1)TP$$
(33)

Below bubble point, the 'oil' phase is saturated with dissolved gas and its composition varies as pressure decreases and more light hydrocarbon come out of solution. The density of this 'live' oil is given by:

 $R_{G} = 2.03 [Pe^{(0.02878API - 0.00377T)}]^{1.205}$

$$\rho_{\rm oil} = \frac{(\rho_{\rm o} + 0.0012 \,{\rm GR}_{\rm G})}{B_{\rm o}} \tag{34}$$

where

(35)

and
$$B_o = 0.972 + 0.00038 \left[2.4 R_G \sqrt{\frac{G}{\rho_o}} + T + 17.8 \right]^{1.175}$$
 (36)

The velocity can be calculated by replacing ρ_o in (33) with a pseudo density ρ' representing the expansion caused by gas intake:

$$\rho' = \frac{\rho_o}{B_o(1 + 0.001R_G)}$$
(37)

in both cases, the bulk modulus is calculated from density and velocity by

$$\mathbf{K}_{\rm oil} = \rho_{\rm oil} \mathbf{V}_{\rm oil}^{2} \tag{38}$$

which is equivalent to Eq (2a) because fluids do not have any shear strength.



Figure 3.1 Location map of the two oil fields off-shore Louisiana presented in this paper. The LF sand, Eugene Island Block 330, produced 130,000 m³ of oil and 40 million m³ of gas between two 3D surveys shot in 1985 and 1992. The K8 sand, South Timbalier Block 295, produced 350,000 m³ of oil and 150 millions m³ of gas between surveys in 1988 and 1994. The grey areas show the actual overlap between successive surveys that were used in the 4D analysis.



Figure 3.2 (a) Structure of the top of the K8 reservoir, South Timbalier 295. The reservoir dips slightly to the South West and leans on a paleohigh to the east. A12 and A22 are the two wells producing between the 1988 and 1994 surveys (**b**) North South cross-section of the K8 reservoir. The grid represents the grid used in the simulation. Colors show the porosity, estimated by stochastic simulation.



Figure 3.3: (a) Oil and (b) gas production history of the two wells producing from the K8 reservoir. The Bottom Hole Pressures (BHP) measured in A12 illustrates the increase in GOR and in gas production when reservoir pressure falls below bubble point at the beginning of 1993.



Figure 3.4: Results of the impedance inversion of 3D seismic surveys of K8 in 1988 (a) and 1994 (b). The layers are numbered from bottom to top, referring to the grid shown in Figure 3.2b. By convention, for consistency with the seismic 'brightening' usually associated with free gas, low impedance values are in red and high impedance in blue.
(c) Difference between the two impedance inversions. Impedance decrease between 1988 and 1994 is in red. In this figure, as in all the following representations of the reservoir, the two producing wells are indicated by the black lines.



Figure 3.5: Pressure distribution estimated in K8 before the beginning of production in 1989, assuming that the reservoir was in hydrostatic equilibrium. The vertical dimension of the elements is exagerated in this figure to enhance configuration of the grid used in the simulation.



Figure 3.6: Results of the stochastic reservoir characterization of K8: (a) porosity (b) shaliness. For visual coherence between the two figures, high shaliness (low sand content and low porosity) is in blue. In addition to the two producing wells (purple), the other wells used for the calibration of the reservoir characterization are shown (black).



Figure 3.7: Comparison of the predictions of the various petrophysic models with the impedance inversion of 1988, before production. (a) KT, (b) Gassamnn+KT, (c) Han, (d) Gassmann+Han and (e) Gassmann+Ramamoorthy. Equations of the linear fits and regression coefficients (R) are given in each figure.



Figure 3.8: Evolution of the reservoir impedance distribution in the case of a uniform sweep of the reservoir. (a) Impedances calculated before production, when the reservoir fluids are in hydrostatic equilibrium. Oil saturation is uniformly 70%, the rest of the pore space corresponds to connate water. (b) Impedance distribution if the gas cap had migrated uniformly downdip to 3280 mbsf between 1989 and 1994. (c) Change in impedance that would be observed in this simple case. The comparison with the inversion results (Fig 3.4c) shows that the reservoir behavior is more complex.



Figure 3.9: (a) Relationship between permeability and porosity measured on 26 sidewall cores collected in K8. The equation of the exponential fit is used to define the permeability distribution in K8.(b) Gas/Oil saturation function. (c) Oil/Water saturation function



Figure 3.10: Permeability distribution in K8, calculated from the results of the reservoir characterization and the permeability/porosity relationship derived from K8 core samples. All the wells used for the reservoir characterization are shown.



Figure 3.11: Comparison between observed and simulated (**a**) oil and (**b**) gas productions in K8. Filled circles represent the observed data shown in Figure 3.3, and lines are simulation results. In (**c**) evolution of the field pressure (Black line) can be compared with the few BHPs available.



Figure 3.12: Oil migration stream line in K8 at various dates (**a**) 05/92, (**b**) 01/93, (**c**) 05/93, (**d**) 08/92. The lines are not actual particule trajectories, but represent the velocity field at each time. The background color pattern is the porosity distribution at the bottom of the reservoir.



Figure 3.13: Pressure distribution in the reservoir at the same times as in figure 3.12.



Figure 3.14: (a) Oil and (b) gas saturation at the end of the simulation of K8 in 1994. At the beginning of the simulation, they were uniformly 70% and 0%, respectively.



Figure 3.15: Impedances calculated from the simulation results in K8 in 1988 (a), and in 1994 (b). (c) Difference between the two time steps.



5.8

5.6

5.4

5.2

5.0

4.8

4.6 ∟ 4.6

5.8

 $\begin{array}{c} \text{Model Impedance } (10^{6}\,\text{kg.m}^{-2_{s}^{-1}}) \\ \text{8} \\ \text{8} \\ \text{8} \\ \text{7} \\ \text{7} \\ \text{8} \\ \text{8}$

Model Impedance (10⁶ kg.m⁻²s⁻¹)

a) KT

y = 0.778

5.0

4.8

c) Han

y

= 0.720



Figure 3.16: Comparison of impedances calculated with the various elastic models at the end of the simulation with the impedance inversion of 1994 (a) KT (b) Gassamnn+KT, (c) Han, (d) Gassmann+Han and (e) Gassmann+Ramamoorthy. (f) Crossplot of the two inversion results. Equations of the linear fits and regression coefficients (R) are indicated in each figure.







Figure 3.18: Production history from the fault block B in the LF sand. (a) Oil and (b) gas production rates in the downdip block 331. Production in this Block stopped in 1980.(c) Oil and (d) Gas production in Block 330. Seven wells were producing from each block.



Figure 3.19: Impedance inversion results in the LF sand in 1985 (a) and1992 (b).(c) Difference between the two inversions. Color convention are the same as in Fig. 3.4, red indicating low impedance in (a) and (b) and decrease in impedance in (c).

5.4

Impedance

 $(10^{6} \text{ kg.m}^{2}.\text{s}^{-1})$

6.2

4.6

4.6

5.4

Impedance $(10^6 \text{ kg.m}^2.\text{s}^{-1})$

6.2

-0.2

0.0

Impedance Change

 $(10^6 \text{ kg.m}^2.\text{s}^{-1})$

0.2



Figure 3.20: (a) Porosity, (b) shaliness and (c) permeability distributions in the LF sand. The shaliness was determined by geostatistical simulation. Porosity was calculated by a time-average relationship using the 1992 impedance and the shaliness. The blue areas in the porosity distribution indicate the actual limits of the fault block B, bounded by two sealing faults to the north and to the south. The producing wells are purple. Additionnal wells used to constrain the reservoir characterization are also shown in black.



Figure 3.21: Permeability/Porosity relationship measured on 250 core samples from the LF sand. The equation of the least square exponential fit was used to calculate the permeability distribution in the reservoir model.



Figure 3.22: Results of the production history match in the LF sand. (a) Oil and (b) gas history match in Block 331. (c) Oil and (d) gas history match in Block 330. Diamonds are the observed data shown in Figure 3.18. Lines are simulated production.
(e) Comparison of the simulated BHPs with the BHPs collected during the history of the reservoir. Because the location of most data (diamonds) were not available, they are only indicators of the global reservoir pressure evolution. Green and red lines indicate simulated pressures from the wells in Blocks 331 and 330 respectively. The thick black line shows the evolution of the average reservoir pressure.



Figure 3.23: Simulated oil saturation in the LF sand in (a)1985 and (b) 1992.
(c) Difference between (a) and (b), indicating the changes in oil saturation between the two 3D seismic surveys. In this figure and the following ones, the resolution of the original volume has been upscaled by 3, corresponding to the actual resolution of the simulator. The layer numbers refer to the upscaled model layers.



Figure 3.24: Simulated gas saturation in the LF sand in 1985 (a) and 1992 (b).(c) Difference between (a) and (b), indicating the changes in gas saturation between the two 3D surveys.



Figure 3.25: Impedances calculated from the simulation results in LF at the time of the 3D seismic surveys in 1985 (a) and in 1992 (b). (c) Simulated impedance difference between the two surveys.