

```

% gda07_01
% depicts a 3D box containing a vector
% support Figure 7.1

clear all;

% independent variable x
Nx = 51;
xmin = 0;
xmax = 1;
Dx = (xmax-xmin)/(Nx-1);
x = xmin + Dx*[0:Nx-1]';

% independent variable y
Ny = 51;
ymin = 0;
ymax = 1;
Dy = (ymax-ymin)/(Ny-1);
y = ymin + Dy*[0:Ny-1]';

% independent variable z
Nz = 51;
zmin = 0;
zmax = 1;
Dz = (zmax-zmin)/(Nz-1);
z = zmin + Dz*[0:Nz-1]';

% make grid
[XX, YY, ZZ] = meshgrid( x, y, z );

% model parameter graph

% make a "ball" in 3-space by contouring
% a Normal distribution centered on the
% center of the ball

% parameters for Normal distribution
rbar = [0.7, 0.8, 0.9]';
sd=0.1;
C = (sd^2)*eye(3,3);
CI = inv(C);
DC = det(C);
norm = ( ((2*pi)^(3/2)) * sqrt(DC) );

% normal distribution
PP = zeros(Nx,Ny,Nz);
for i=[1:Nx]
for j=[1:Ny]
for k=[1:Nz]
    r = [XX(i,j,k), YY(i,j,k), ZZ(i,j,k)]';
    PP(i,j,k) = exp(-0.5*(r-rbar)'*CI*(r-rbar))/norm;
end
end
end

figure(1);
clf;
set(gca, 'LineWidth',3);
set(gca, 'FontSize',14);

```

```

hold on;
axis( [xmin, xmax, ymin, ymax, zmin, zmax]');

% improvise outline of 3D box
plot3( [xmin,xmin], [ymin,ymin], [zmin,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmin,xmin], [ymin,ymax], [zmin,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmin,xmax], [ymin,ymin], [zmin,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmax], [ymax,ymax], [zmax,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmax], [ymax,ymin], [zmax,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmin], [ymax,ymax], [zmax,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmin], [ymin,ymin], [zmax,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmax], [ymin,ymin], [zmax,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmin,xmin], [ymax,ymin], [zmax,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmin,xmin], [ymax,ymax], [zmax,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmax], [ymax,ymin], [zmin,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmin], [ymax,ymax], [zmin,zmin], 'k-', 'LineWidth', 2 );
xlabel('m_1');
ylabel('m_2');
zlabel('m_3');

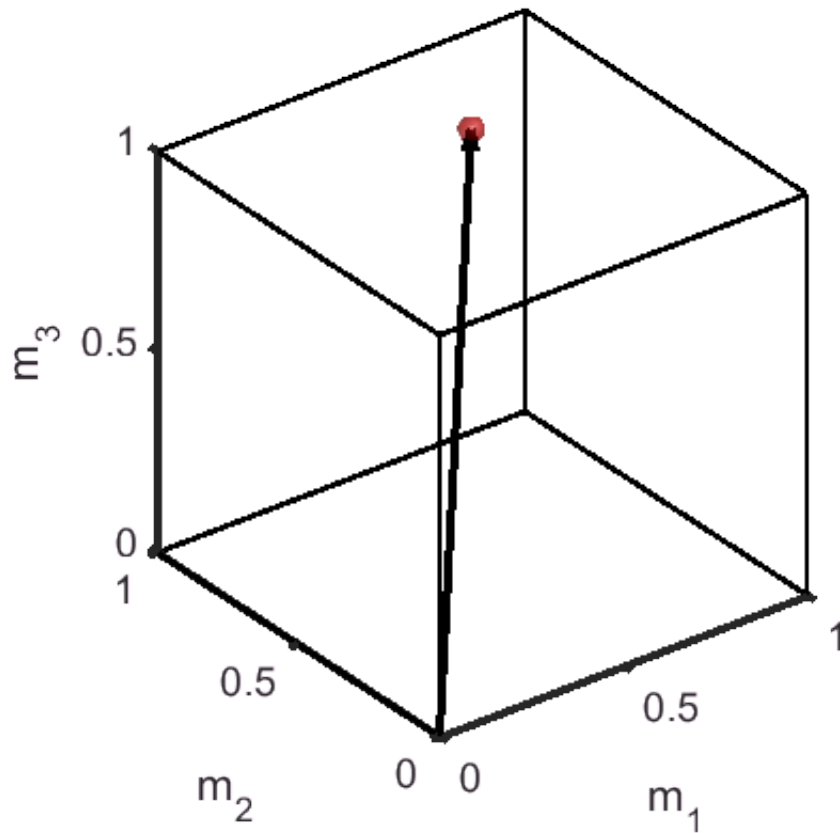
% plot a line representing a vector
maxP=max(max(max(PP)));
plot3( [0, rbar(1)], [0, rbar(2)], [0, rbar(3)], 'k-', 'LineWidth', 3 );

% pretty crazy way to draw an arrowhead!
tangent = rbar/sqrt(rbar'*rbar);
per1 = cross( tangent, [0, 0, 1]' );
per1 = per1/sqrt(per1'*per1);
per2 = cross( tangent, per1 );
per2 = per2/sqrt(per2'*per2);
L = 0.05;
v1 = rbar - L*tangent + 0.25*L*per1;
v2 = rbar - L*tangent - 0.25*L*per1;
v3 = rbar - L*tangent + 0.25*L*per2;
v4 = rbar - L*tangent - 0.25*L*per2;
plot3( [rbar(1), v1(1)], [rbar(2), v1(2)], [rbar(3), v1(3)], 'k-', 'LineWidth', 3 );
plot3( [rbar(1), v2(1)], [rbar(2), v2(2)], [rbar(3), v2(3)], 'k-', 'LineWidth', 3 );
plot3( [rbar(1), v3(1)], [rbar(2), v3(2)], [rbar(3), v3(3)], 'k-', 'LineWidth', 3 );
plot3( [rbar(1), v4(1)], [rbar(2), v4(2)], [rbar(3), v4(3)], 'k-', 'LineWidth', 3 );

% contour the ball
p=patch(isosurface( XX, YY, ZZ, PP, 0.95*maxP ));
isonormals(XX,YY,ZZ,PP, p)
set(p, 'FaceColor', 'red', 'FaceAlpha', 0.5, 'EdgeColor', 'none');

% set view, lighting, etc
daspect([1 1 1])
view(3)
camlight; lighting phong

```



% Figure 7.1 (A) The model parameters represented as a vector  $m$  in the  $M$ -dimensional space  $S(m)$  of all possible model parameters. MatLab script gda07\_01.

```
% data graph
```

```
% parameters for Normal distribution
```

```
rbar = [0.9, 0.6, 0.7]';
```

```
sd=0.1;
```

```
C = (sd^2)*eye(3,3);
```

```
CI = inv(C);
```

```
DC = det(C);
```

```
norm = ( ((2*pi)^(3/2)) * sqrt(DC) );
```

```
% Normal distribution
```

```
PP = zeros(Nx,Ny,Nz);
```

```
for i=[1:Nx]
```

```
for j=[1:Ny]
```

```
for k=[1:Nz]
```

```
    r = [XX(i,j,k), YY(i,j,k), ZZ(i,j,k)]';
```

```
    PP(i,j,k) = exp(-0.5*(r-rbar)'*CI*(r-rbar))/norm;
```

```
end
```

```
end
```

```
end
```

```
figure(2);
```

```
clf;
```

```
set(gca,'LineWidth',3);
```

```
set(gca,'FontSize',14);
```

```
hold on;
```

```
axis( [xmin, xmax, ymin, ymax, zmin, zmax]');
```

```

% improvise outline of 3D box
plot3( [xmin,xmin], [ymin,ymin], [zmin,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmin,xmin], [ymin,ymax], [zmin,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmin,xmax], [ymin,ymin], [zmin,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmax], [ymax,ymax], [zmax,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmax], [ymax,ymin], [zmax,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmin], [ymax,ymax], [zmax,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmin], [ymin,ymin], [zmax,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmax], [ymin,ymin], [zmax,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmin,xmin], [ymax,ymin], [zmax,zmax], 'k-', 'LineWidth', 2 );
plot3( [xmin,xmin], [ymax,ymax], [zmax,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmax], [ymax,ymin], [zmin,zmin], 'k-', 'LineWidth', 2 );
plot3( [xmax,xmin], [ymax,ymax], [zmin,zmin], 'k-', 'LineWidth', 2 );
xlabel('d_1');
ylabel('d_2');
zlabel('d_3');

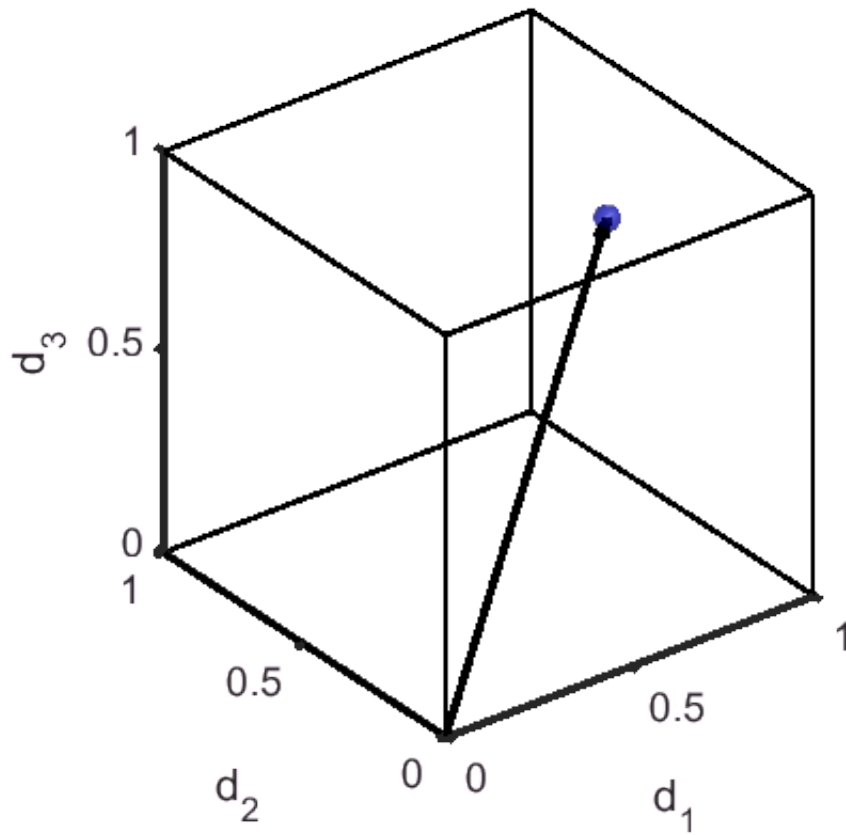
% draw a vector
maxP=max(max(max(PP)));
plot3( [0, rbar(1)], [0, rbar(2)], [0, rbar(3)], 'k-', 'LineWidth', 3 );

% pretty crazy way to draw an arrowhead!
tangent = rbar/sqrt(rbar'*rbar);
per1 = cross( tangent, [0, 0, 1]' );
per1 = per1/sqrt(per1'*per1);
per2 = cross( tangent, per1 );
per2 = per2/sqrt(per2'*per2);
L = 0.05;
v1 = rbar - L*tangent + 0.25*L*per1;
v2 = rbar - L*tangent - 0.25*L*per1;
v3 = rbar - L*tangent + 0.25*L*per2;
v4 = rbar - L*tangent - 0.25*L*per2;
plot3( [rbar(1), v1(1)], [rbar(2), v1(2)], [rbar(3), v1(3)], 'k-', 'LineWidth', 3 );
plot3( [rbar(1), v2(1)], [rbar(2), v2(2)], [rbar(3), v2(3)], 'k-', 'LineWidth', 3 );
plot3( [rbar(1), v3(1)], [rbar(2), v3(2)], [rbar(3), v3(3)], 'k-', 'LineWidth', 3 );
plot3( [rbar(1), v4(1)], [rbar(2), v4(2)], [rbar(3), v4(3)], 'k-', 'LineWidth', 3 );

% contour the ball
p=patch(isosurface( XX, YY, ZZ, PP, 0.95*maxP ));
isonormals(XX,YY,ZZ,PP, p)
set(p, 'FaceColor', 'blue', 'FaceAlpha', 0.5, 'EdgeColor', 'none');

% set view angle, lighting, etc.
daspect([1 1 1])
view(3)
camlight; lighting phong

```



```
% Figure 7.1 (B) The data represented as a vector d in the  
% N-dimensional space S(d) of all possible data. MatLab script gda07_01.
```