

```
% gda05_14
%
% prior distribution pA(d1,m1) interacting with inexact
% theory pg(d1,m1) to produce total distribution pT(d1,m1)
% supports Figure 5.14
```

```
clear all;
```

```
% d1 variable
```

```
Nd1 = 101;
dlmin = 0;
dlmax = 5.0;
Dd1 = (dlmax-dlmin)/(Nd1-1);
d1 = dlmin + Dd1*[0:Nd1-1]';
```

```
% m1 variable
```

```
Nm1 = 101;
mlmin = 0;
mlmax = 5.0;
Dm1 = (mlmax-mlmin)/(Nm1-1);
m1 = mlmin + Dm1*[0:Nm1-1]';
```

```
% setup for distribution P1=PA
```

```
P1=zeros(Nd1,Nm1);
dlbar = 2.25;
mlbar = 2.08;
bar = [dlbar, mlbar]';
sd1 = 0.5;
sm1 = 1;
C1 = diag( [sd1^2, sm1^2]' );
CI1 = inv(C1);
DC1 = det(C1);
% note not normaalized, so max is unity
for i=[1:Nm1]
for j=[1:Nd1]
    x1=[d1(i), m1(j)]' - bar;
    P1(i,j) = exp( -0.5 * x1'*CI1*x1 );
end
end
```

```
% axis for parametric curve s
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```
Ns = 51;
smin = 0;
smax = 5.0;
Ds = (smax-smin)/(Ns-1);
s = smin + Ds*[0:Ns-1]';
```

```
% Pg follows parameric curve
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```
dp = 1+s-2*(s/smax).^2;
mp = s;
```

```
% P2=Pg distribution; not normalizable
```

```
P2 = zeros(Nd1,Nm1);
sg = 0.35;
sg2 = sg^2;
for i=[1:Nm1]
for j=[1:Nd1]
    r2 = (d1(i)-dp).^2 + (m1(j)-mp).^2;
    r2min=min(r2);
```

```

P2(i,j) = exp( -r2min/sg2 );
end
end

% P3=PT is product of PA and Pg
P3 = P1.*P2;
[tmp, itmp] = max(P3);
[P3max, Pj] = max(tmp);
Pi=itmp(Pj);
Pmaxm1 = mlmin+Dm1*(Pj-1);
Pmaxd1 = dlmin+Dd1*(Pi-1);

figure(1);
set(gcf,'pos',[10, 10, 800, 300] );
clf;

% plot PA
subplot(1,3,1);
set(gca,'LineWidth',3);
set(gca,'FontSize',14);
colormap('jet');
hold on;
axis( [dlmin, dlmax, mlmin, mlmax] );
axis ij;
imagesc( [dlmin, dlmax], [mlmin, mlmax], P1 );
plot( mlbar, dlbar, 'wo', 'LineWidth', 3 );
plot( [mlbar, mlbar], [dlmax, dlmax-0.1], 'w-', 'LineWidth', 3 );
plot( [mlmin, mlmin+0.1], [dlbar, dlbar], 'w-', 'LineWidth', 3 );
plot( mp, dp, 'w:', 'LineWidth', 2 );
xlabel('m');
ylabel('d');

% Plot Pg
subplot(1,3,2);
set(gca,'LineWidth',3);
set(gca,'FontSize',14);
colormap('jet');
hold on;
axis( [dlmin, dlmax, mlmin, mlmax] );
axis ij;
imagesc( [dlmin, dlmax], [mlmin, mlmax], P2 );
plot( mp, dp, 'w:', 'LineWidth', 2 );
plot( mlbar, dlbar, 'wo', 'LineWidth', 3 );
plot( [mlbar, mlbar], [dlmax, dlmax-0.1], 'w-', 'LineWidth', 3 );
plot( [mlmin, mlmin+0.1], [dlbar, dlbar], 'w-', 'LineWidth', 3 );
xlabel('m');
ylabel('d');

% plot PT
subplot(1,3,3);
set(gca,'LineWidth',3);
set(gca,'FontSize',14);
colormap('jet');
hold on;
axis( [dlmin, dlmax, mlmin, mlmax] );
axis ij;
imagesc( [dlmin, dlmax], [mlmin, mlmax], P3 );
plot( mp, dp, 'w:', 'LineWidth', 2 );
plot( mlbar, dlbar, 'wo', 'LineWidth', 3 );
plot( Pmaxm1, Pmaxd1, 'ko', 'LineWidth', 3 );
plot( [mlbar, mlbar], [dlmax, dlmax-0.1], 'w-', 'LineWidth', 3 );

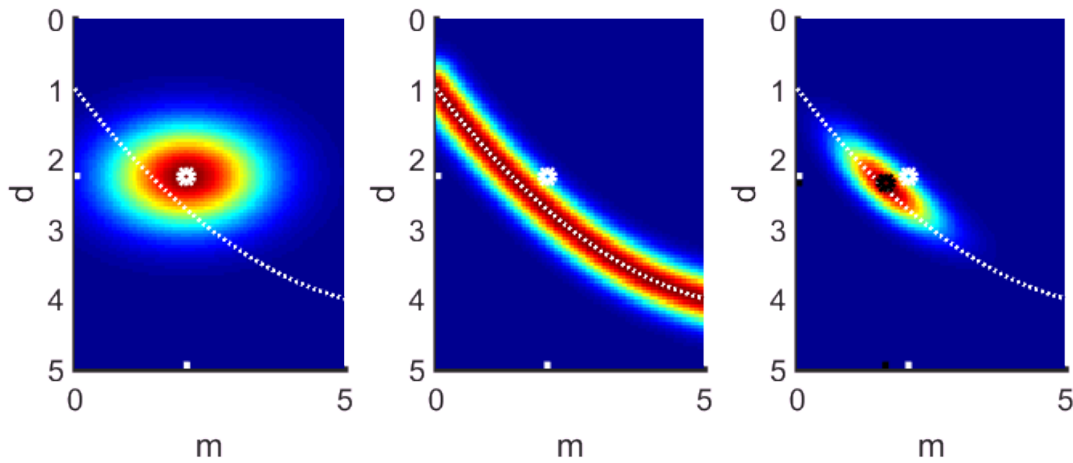
```

```

plot( [mlmin, mlmin+0.1], [dlbar, dlbar], 'w-', 'LineWidth', 3 );
plot( [Pmaxml, Pmaxml], [dlmax, dlmax-0.1], 'k-', 'LineWidth', 3 );
plot( [mlmin, mlmin+0.1], [Pmaxd1, Pmaxd1], 'k-', 'LineWidth', 3 );

xlabel('m');
ylabel('d');

```



% Figure 5.14 (A) The prior probability density function $p_A(m, d)$ represents the state of know
 % the theory is applied. Its mean (white circle) is the prior model parameter map and observed
 % An inexact theory is represented by the conditional probability density function $p_g(m, d)$, w
 % centered about the exact theory (dotted white curve). (C) The product $p_T(m, d) = p_A(m, d)p_g(m, d)$
 % the prior information and theory. Its peak is at the estimated data mest and predicted data